

YMCA UNIVERSITY OF SCIENCE AND TECHNOLOGY
FARIDABAD

M.SC (PHYSICS) SEM-I EXAMINATION (under CBS)

MATHEMATICAL PHYSICS (PHY-101)

Time: 3 hr

M.Marks:60

Note: Note: Part-A consists of Question No.1 which is compulsory. Attempt any four from Part-B.

Part-A

- 1 (a) Separate into real and imaginary parts $\sin(x + iy)$
- (b) What is the necessary and sufficient condition(s) for $f(z)$ to be analytic?
- (c) Differentiate between Simply connected and Multiply connected regions.
- (d) State and prove the change of scale property of Fourier transform.
- (e) Find the Laplace transform of $t \cos at$.
- (f) Find the inverse Laplace transform of $\frac{s^2 - 3s + 4}{s^3}$
- (g) For any matrix A, prove that AA' and $A'A$ are both symmetric.
- (h) What is a Triangular matrix?
- (i) Differentiate between Abelian and non-Abelian group.
- (j) What is the need of integral transforms? (2x10)

Part-B

2. (a) If $u(x, y) = x^2 - y^2$ is the real part of an analytic function $f(z) = u + iv$. find v . (3)
- 2 (b) State and prove Cauchy's Integral Theorem for the function of a complex variable. (4)
- 2 (c) Evaluate $\int_0^{2\pi} \frac{d\theta}{2 + \cos \theta}$ (3)
3. (a) Find the Fourier sine and cosine transform of $x e^{-ax}$ (5)

3 (b) State and prove *Parseval's Identity* for Fourier Transforms. (5)

4. (a) Obtain Laplace transform of the function:

$$\begin{aligned} f(t) &= \sin t, & 0 < t < \pi \\ &= 0, & t \geq \pi \end{aligned} \quad (5)$$

4 (b) Evaluate inverse Laplace transform of $\int_s^\infty \tan^{-1}\left(\frac{2}{s^2}\right) ds$ (5)

5 (a) Derive the Laurent's series expansion for the function of a complex variable. (5)

5 (b) Describe any three properties of Laplace Transforms. (5)

6 (a) Prove that if G be an infinite cyclic group, then G has exactly two generators. (4)

6 (b) If a group has four elements, show that it must be abelian. (3)

6 (c) Show that any two characteristic vectors (Eigen vectors) corresponding to two distinct Eigen values of a Hermitian matrix are orthogonal. (3)

7 (a) Let G be finite non-abelian group of order n with the property that G has a subgroup of order k for each positive integer k dividing n . Prove that G is not a simple group. (5)

7 (b) Prove that

$$\frac{2}{\pi} \int_0^\infty F_s(s) G_s(s) ds = \int_0^\infty f(x) g(x) dx$$

where the symbols have their usual meanings. (5)