

Time: 3 Hours

Max. Marks:60

- Note: 1. It is compulsory to answer the questions of **Part-A**. Limit your answers within 20-40 word in this part.
 2. Answer any four questions from **Part -B** in detail.
 3. Different parts of the same question are to be attempted adjacent to each other.
 4. Use of non-programmable simple calculator is allowed.
 5. Assume suitable standard data wherever required, if not given.

Part-A

- Q1 (a) Obtain the Hermitian conjugate of the operator $x \frac{d}{dx}$. (2)
- (b) Describe Hilbert space. (2)
- (c) Prove the following commutation relations: (2)
- $$[x, p_x] = 0$$
- $$[z, p_z] = i\hbar$$
- (d) Discuss the completeness condition. (2)
- (e) Obtain the commutation relation between L_+ and L_- . (2)
- (f) For Pauli spin matrices, prove that $\sigma_x \sigma_y = 2i\sigma_z$. (2)
- (g) Define differential and total scattering cross-section. (2)
- (h) Discuss the validity of Born approximation. (2)
- (i) Explain Zeeman effect using perturbation theory. (2)
- (j) What is Harmonic perturbation. (2)

Part-B

- Q2 (a) Define basis and operators in quantum mechanics. (6)
- (b) Define projection operator and obtain P_a^2 . (4)
- Q3 (a) Explain Schrödinger's picture. Obtain the time derivative of the expectation value of an observable in it. (6)
- (b) Consider the states $|\psi_1\rangle = |\phi_1\rangle + 2|\phi_2\rangle + 3|\phi_3\rangle$ and $|\psi_2\rangle = a|\phi_1\rangle + 4|\phi_2\rangle + 2|\phi_3\rangle$, where $|\phi_1\rangle, |\phi_2\rangle$ and $|\phi_3\rangle$ are orthonormal kets. Find the constant 'a' such that $|\psi_1\rangle$ & $|\psi_2\rangle$ are orthogonal. (4)
- Q4 Define raising and lowering operators J_+ and J_- using representation in which J^2 and J_z are diagonal. Also obtain the matrix element for J_x and J_y . (10)
- Q5 Find the matrix representation for angular momentum operators J^2 and J_z . Obtain the eigen values for J^2 and J_z operators when spin $j = 3/2$ and $j = 1$. (10)
- Q6 (a) Calculate the differential scattering cross-section in the Born approximation for the scattering of a particle by an attractive square well potential: (6)
- $$V(r) = \begin{cases} -V_0 & \text{for } r < a \\ 0 & \text{for } r > a \end{cases}; \text{ where } V_0 > 0.$$
- (b) Derive an expression for phase shift using partial wave method. (4)
- Q7 (a) Discuss the time independent perturbation theory for non-degenerate systems and obtain the expression for first order correction to energy. (6)
- (b) Explain Fermi Golden rule for the rate of transition to a continuum of final states due to constant perturbation. (4)
