

Sr. No 322304

Dec-2023

B.Sc. (Chemistry) 3rd Sem.

Statistics and Infinite Series (OMTH-302)

Time: 3 Hours

Max. Marks:75

- Instructions:**
1. It is compulsory to answer all the questions (1.5 marks each) of Part -A in short.
 2. Answer any four questions from Part -B in detail.
 3. Different sub-parts of a question are to be attempted adjacent to each other.

PART-A

- Que.1(a) Find tenth term of the A.P. whose first term is 5 and common difference is 2.
- (b) Is 90 a term of the series $4 + 7 + 10 + 13 + \dots$?
- (c) Explain bounded sequence with examples.
- (d) Define independent events. Also give two examples.
- (e) If the fifth term of a G.P. is 162 and the first term is 2, then find the common ratio.
- (f) A bag contains 6 white balls, 9 black balls. What is the probability of drawing a black ball?
- (g) What is the probability of getting a total of more than 10 in a single throw with two dice?
- (h) What is positive term series? Explain.
- (i) Examine the nature of the series $1 + 2 + 3 + 4 + \dots + n + \dots + \infty$.
- (j) Test the nature of the series $1 + (3/4) + (9/16) + (27/64) + \dots + \infty$. (1.5*10=15)

PART-B

Q.2(a) Calculate the arithmetic mean of the number of florets on sunflower as given below:

Class interval	Frequency	Class Interval	Frequency
10-20	2	50-60	29
20-30	7	60-70	10
30-40	17	70-80	3
40-50	29	80-90	2
		90-100	1

(7)

(b) In a study on patients, the following data was obtained. Find the standard deviation of the data.

Age(in years):	10-19	20-29	30-39	40-49	50-59	60-69	70-79	80-89
Number of Cases:	1	0	1	10	17	38	9	3

(8)

Q.3(a) The sum of 'p' terms of a series is $2p^2 + p$. Prove that the series is in A.P. (7)

(b) The sum of the digits of a three digit number is 12. The digits are in A.P. If the digits are reversed, then the number is diminished by 396. Find the number. (8)

Q.4(a) If $3x+1$, $7x$ and $10x+8$ be in G.P., then find the value of x. (7)

(b) Find the sum of the given series:

(i) $2+6+18+54+\dots$ to 10 terms.

(ii) $1 - \frac{1}{2} + \frac{1}{4} - \frac{1}{8} + \dots$ to 12 terms. (8)

Q.5(a) The probability that a student passes a physics test is $(\frac{2}{3})$ and the probability that he passes both physics and English test is $(\frac{14}{45})$. The probability that he passes at least one test is $(\frac{4}{5})$. What is the probability that the student passes the English test. (7)

(b) The probability that a boy will get a scholarship is 0.9 and that a girl will get is 0.8. What is the probability that at least one of them will get the scholarship? (8)

Q.6(a) Prove that the given series $\frac{2}{3!} + \frac{3}{4!} + \frac{4}{5!} + \dots$ is convergent and find its sum. (7)

(b) Examine the convergence of the series: $\frac{\sqrt{2}-1}{3^3-1} + \frac{\sqrt{3}-1}{4^3-1} + \frac{\sqrt{4}-1}{5^3-1} + \dots$ (8)

Q.7(a) If a, b, c, are in A.P., then prove that $a^2(b+c)$, $b^2(c+a)$, $c^2(a+b)$ are in A.P. (7)

(b) There are 4 boys and 2 girls in room A and 5 boys and 3 girls in room B. A girl from one of the two rooms laughed loudly. What is the probability that the girl who laughed was from room B. (8)