December 2023 B.Tech. EIC Vth SEMESTER Modern Control System (EI 502)

Time: 3 Hours

Max. Marks:75

Instructions:

- 1. It is compulsory to answer all the questions (1.5 marks each) of Part -A in short.
- 2. Answer any four questions from Part -B in detail.
- 3. Different sub-parts of a question are to be attempted adjacent to each other.
- 4. Assume any missing data

PART-A

- Q1 (a) List the demerits of classical control theory. (1.5)
 - (b) What are eigen values? State its significance. (1.5)
 - (c) Define state observers. (1.5)
 - (d) What are the factors that influence the choice of state variables in a dynamic (1.5) system?
 - (e) Differentiate between transfer matrix and transfer function. (1.5)
 - (f) State the necessary condition for carrying pole placement design. (1.5)
 - (g) What are the parameters for designing state observers? (1.5)
 - (h) Define multivariable systems. (1.5)
 - (i) What do you mean by integral control? What it its impact on state feedback? (1.5)
 - (j) How the controllability of discrete time systems is determined? (1.5)

PART-B

Q2 (a) Obtain the transfer function for the system (08)

$$\begin{bmatrix} \dot{x}_{1} \\ \dot{x}_{2} \\ \dot{x}_{3} \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -2 & -3 \end{bmatrix} \begin{bmatrix} \chi_{1} \\ \chi_{2} \\ \chi_{3} \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} u$$

$$y = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} \chi$$

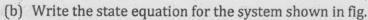
(b) A single input single output system is given by (07)

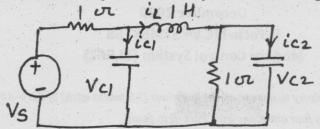
$$\dot{x}(t) = \begin{bmatrix} -1 & 0 & 0 \\ 0 & -2 & 0 \\ 0 & 0 & -3 \end{bmatrix} x(t) + \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} u$$

$$y = \begin{bmatrix} 1 & 0 & 2 \end{bmatrix} x(t)$$

Test for controllability and observability.

Q3 (a) State the properties of state transition matrix.





Q4 (a) Consider a system
$$\dot{x} = \begin{bmatrix} 1 & 1 & 0 \\ 0 & -2 & 1 \\ 0 & 0 & -1 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \\ -2 \end{bmatrix} u \quad y = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} x$$
(08)

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Find the eigenvalues of A and determine the stability of system.

$$\dot{X} = \begin{bmatrix} -3 & 1 \\ 0 & -2 \end{bmatrix} X + \begin{bmatrix} 1 \\ 2 \end{bmatrix} u \quad Y = \begin{bmatrix} 2 & 1 \end{bmatrix} X$$

Design a feedback controller that places the closed loop poles at s= -3+-j4

- Q5 (a) Explain pole placement using state feedback. Discuss the principle of feedback (05) controller design.
 - (b) What is the effect of addition of observer on closed loop system? Also derive (10) the transfer function of observer-based controller.

$$\dot{X} = \begin{bmatrix} 0 & 2 \\ 0 & 2 \end{bmatrix} X + \begin{bmatrix} 0 \\ 2 \end{bmatrix} U \quad Y = \begin{bmatrix} 1 & 0 \end{bmatrix} X$$

Design an observer with poles at s=-8,-8.

- (b) What do you mean by linear discrete state space model? How state variable analysis is done for such systems?
- Q7 (a) Given a block diagram of the system, explain the method of obtaining its state (07) model.
 - (b) What do you mean by canonical form of state model? List the features. (08)
