## January 2023

## B.Sc. (Animations) Re-Appear 1st Semester <br> Mathematics-I (BSC-A18-102)

Instructions :

1. It is compulsory to answer all the questions (1.5 marks each) of Part-A in short.
2. Answer any four questions from Part-B in detail.
3. Different sub-parts of a question are to be attempted adjacent to each other.

## PART-A

1. (a) Find the distance between the points whose coordinates are $(5,2)$ and $(7,3)$.
(b) Identify the following operations as commutative or non-commutative: Matrix addition, matrix subtraction, matrix multiplication.
(c) What is purpose of directrix in ellipse?
(d) Find the equation of a circle that has radius $r$ and its center at the point $(\boldsymbol{h}, \boldsymbol{k})$.
(e) Find the equation of the line joining $(2,5)$ and $(10,20)$.
(f) Find the ratio in which the line joining $\mathrm{A}(5,1,6)$ and $\mathrm{B}(3,4,1)$ is divided by $y z$ plane.
(g) Let $\mathbf{V 1}=\mathbf{2 1} \mathbf{-} \mathbf{J}+\mathbf{K}$ and $\mathbf{V} \mathbf{2}=\mathbf{I}+\mathbf{J} \mathbf{- K}$. Find the angle between V1 and V2.
(h) Find the components of the vector A whose tail is at $\mathrm{P} 1(1,2)$ and whose head is at $\mathrm{P} 2(3,5)$.
(i) Write the matrix for the following transformation :
(i) Rotation in 2D.
(ii) Reflection in 2D both across X and Y axis.
(iii) Scaling in 2D.
(j) Write the transformation matrices for creating the projection in $\mathrm{X}, \mathrm{Y}$ and Z planes.

## PART-B

2. (a) The transformation, $R$, is a reflection in the line $y=-x$. Write down the matrix which represents R .
(b) Write down the matrix for the transformation, L , an enlargement, centre O and scale factor 2 .
(c) The matrix, $Q$, represents a combination of the transformation R , followed by the transformation $\qquad$ Write down the matrix, Q , as a product of the two matrices found in (a) and (b) above.
3. (a) Define three types of Cartesian, spherical and cylindrical coordinate systems. How a point $p(x, y, z)$ in Cartesian coordinate system can be mapped (converted) in other two coordinate systems.
(b) Find the equation of a circle with centre as $(0,0)$ and the straight line $3 x+y-10=0$ as tangent.
4. (a) Perform the rotation of a unit cube about $\boldsymbol{y z}$ plane by $30^{\circ}$
(b) Describe how isometric projection can be created in Z-plane.
5. (a) Find the equation of the straight line perpendicular to $3 x+4 y-10=0$ and passing through the point $(5,6)$.
(b) Find the coordinates of a point dividing the line joining $(10,20)$ and $(30,50)$ in the ratio $2: 3$.
6. (a) Consider a triangle with vertices as $\mathrm{A}(4,1), \mathrm{B}(5,2)$, $\mathrm{C}(4,2)$. Rotate it by $90^{\circ}$ about point A .
(b) Use vector method to show that $\mathrm{P}, \mathrm{Q}, \mathrm{R}$ are Collinear -$\mathrm{P}(3,-5,1), \mathrm{Q}(-1,0,8)$ and $\mathrm{C}(7,-10,-6)$.
7. (a) Write short notes on the following :
(i) Isometric Projection.
(ii) Perspective Projection.
(iii) Anti-aliasing.
